

Scattering Applications with the Time-dependent Basis Function Approach

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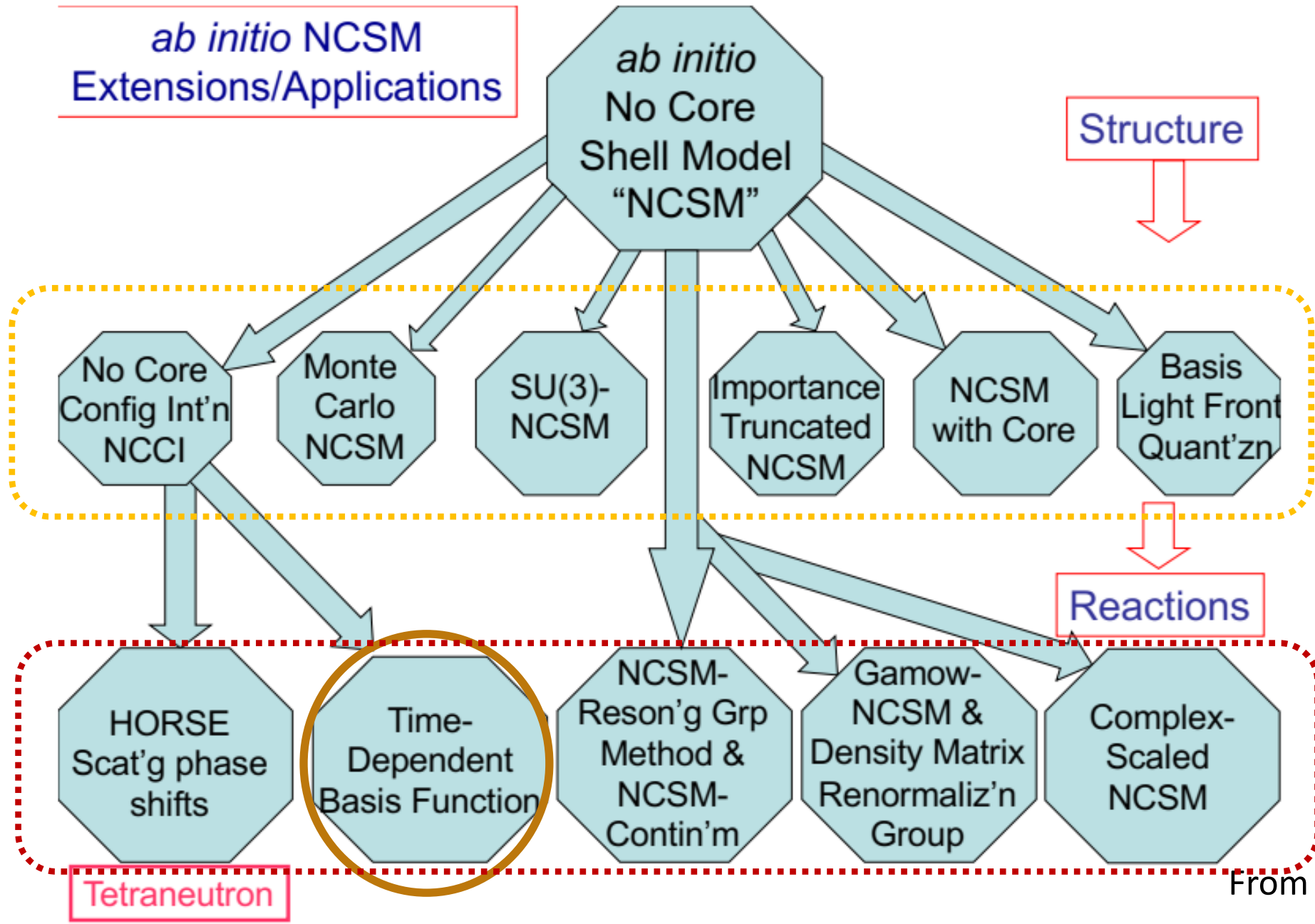
Collaborators

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Motivations for time-dependent basis function (tBF) approach

- Develop nuclear reaction theory based on *ab initio* nuclear structure calculations, e.g., no-core shell model (NCSM)
- Full quantal coherence and non-perturbative couplings among all possible elastic and inelastic processes
- This could enable promising avenues of research to:
 - ❖ Probe *ab initio* nuclear structure results [e.g., $B(E1)$] with external time-dependent Coulomb+nuclear forces
 - ❖ Investigate “forbidden” transitions resulting from non-perturbative processes.
 - ❖ Compare with experimental cross section data



From James P. Vary

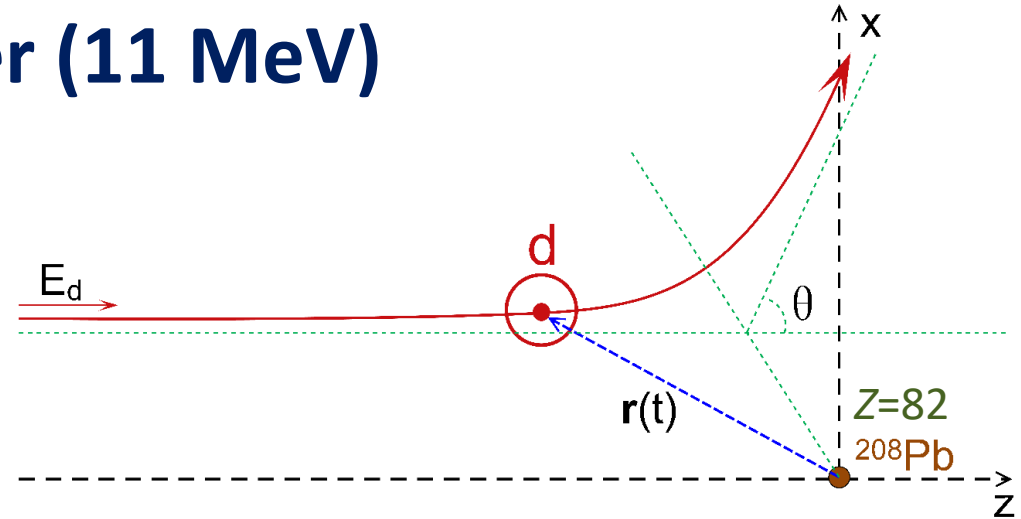
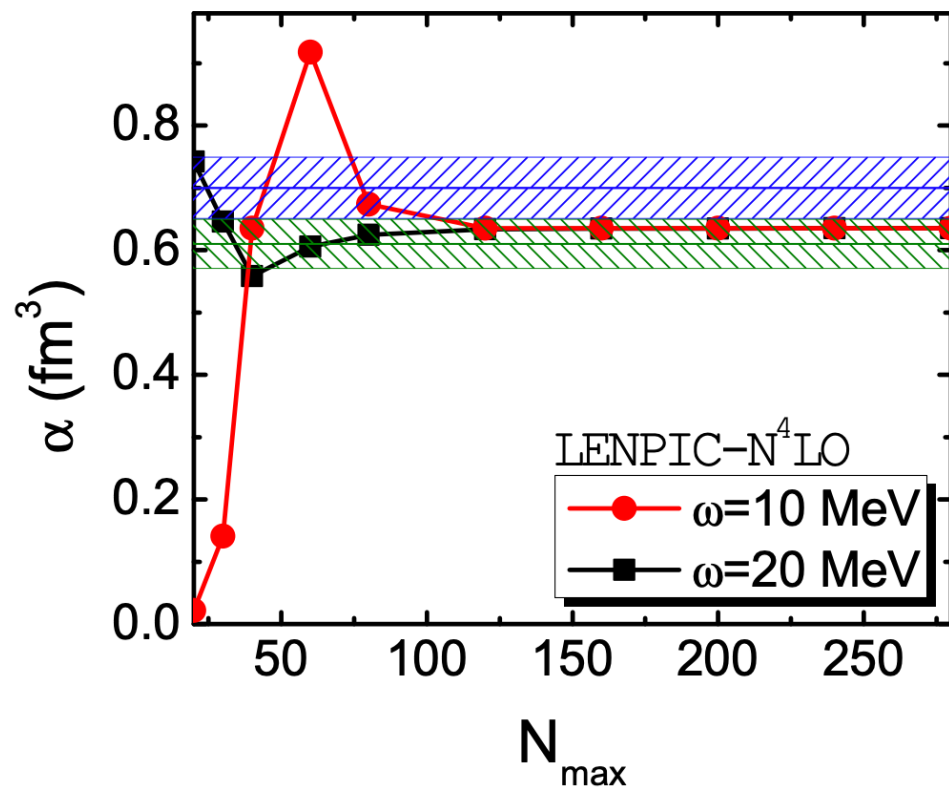
$d+^{208}\text{Pb}$ scatterings below Coulomb barrier (11 MeV)

Solving EOM for CM motion of deuteron in external field:

$$V = V_{\text{coul}} + V_{\text{pol}}$$

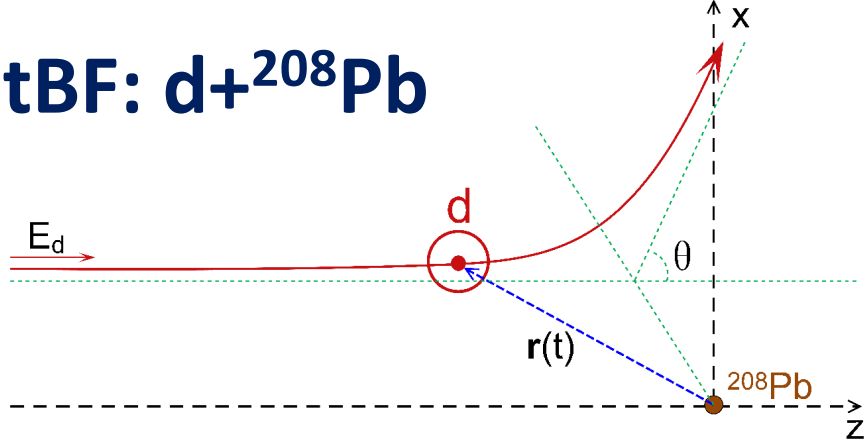
$$V_{\text{pol}} = -\frac{1}{2} \alpha Z^2 e^2 \frac{1}{r^4}$$

$$\alpha = \frac{8\pi}{9} \sum_{n \neq 0} \frac{B(E1; 0 \rightarrow n)}{(E_n - E_0)}$$



- Harmonic oscillator (HO) basis;
- Parameters of HO basis:
 N_{max} and ω , ($2n + 1 \leq N_{\text{max}}$);
- α is converged with respect to N_{max} and ω ;
- LENPIC interactions:
regulator $R=1.0$ fm.

tBF: d+²⁰⁸Pb



Time-independent:

$$H_0 = T_{\text{rel}} + V_{\text{np}}$$

$$H_0 |\beta_i\rangle = E_i |\beta_i\rangle$$

Basis set $\{|\beta_j\rangle\}$

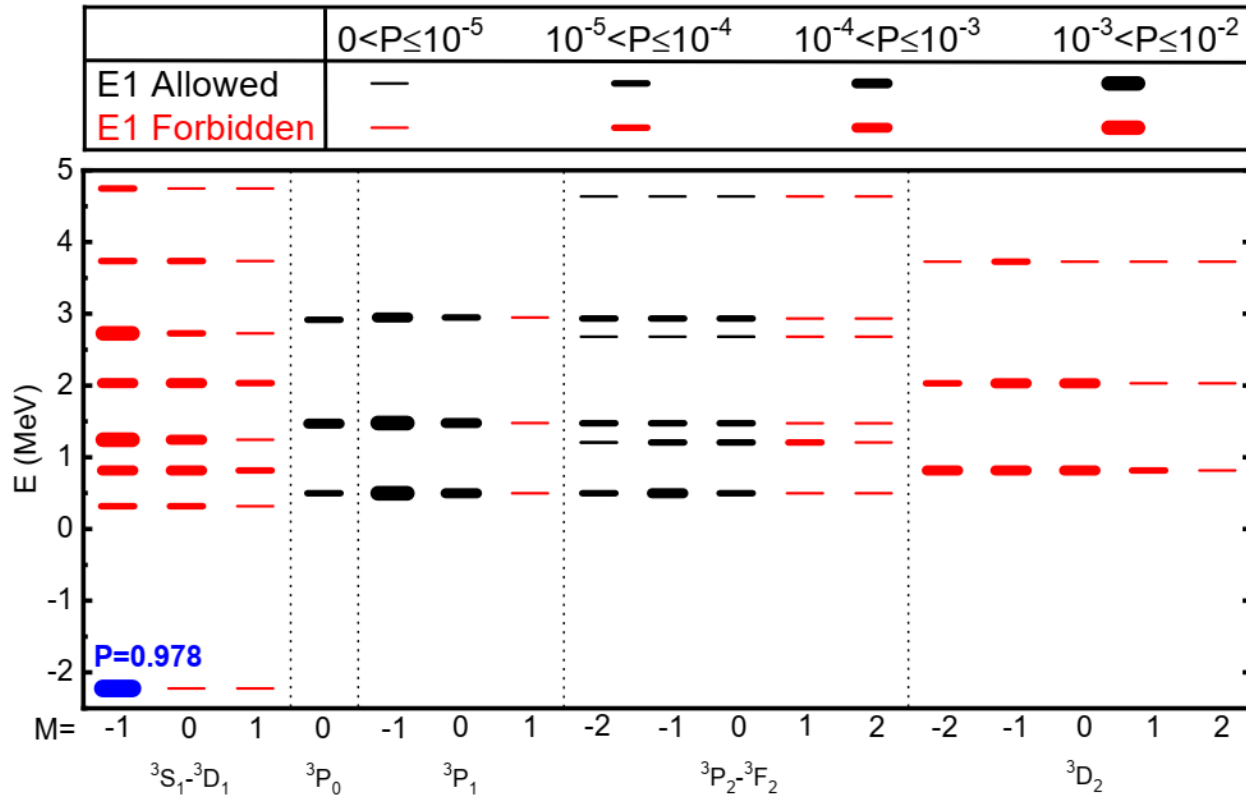
$$H(t) = H_0 + V(t)$$

E1 is dominant

Time-dependent:

$$i \frac{\partial}{\partial t} |\psi(t)\rangle_I = V_I(t) |\psi(t)\rangle_I$$

$$|\psi(t)\rangle_I = \sum_{j=1}^n A_j^I(t) |\beta_j\rangle$$



[Peng Yin *et al.*, in preparation]

- NN interaction: LENPIC-N⁴LO
- HO basis: $N_{\text{max}}, \omega = 20 \text{ MeV}$
- $S=1, J_{\text{max}}=2$

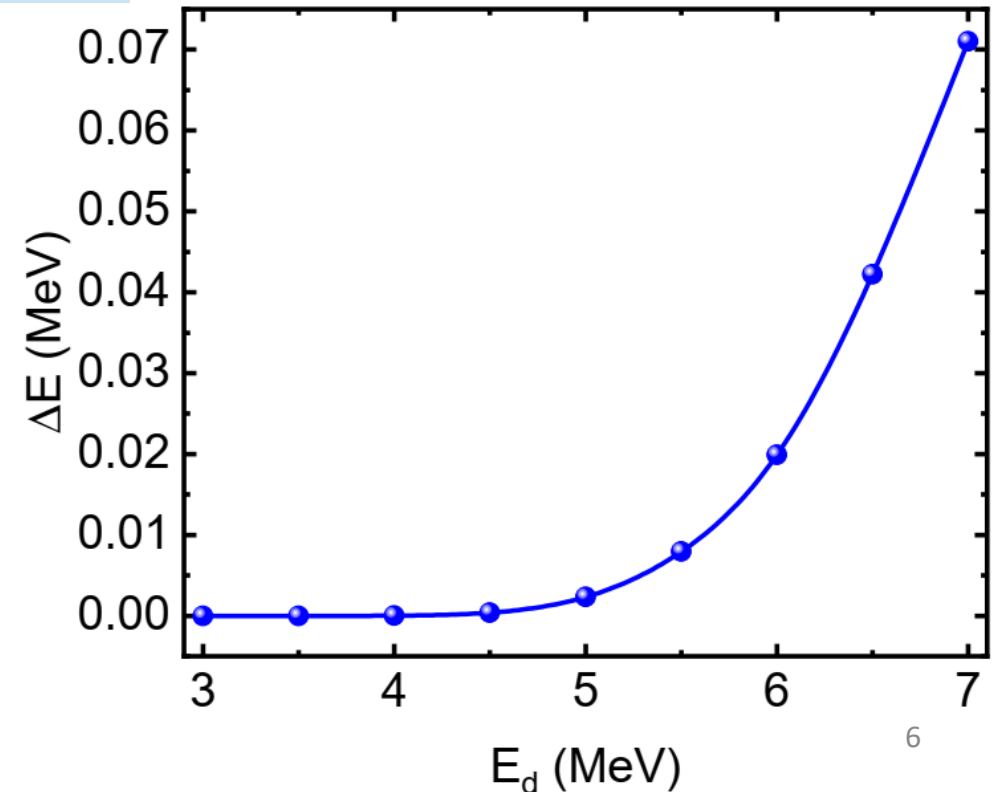
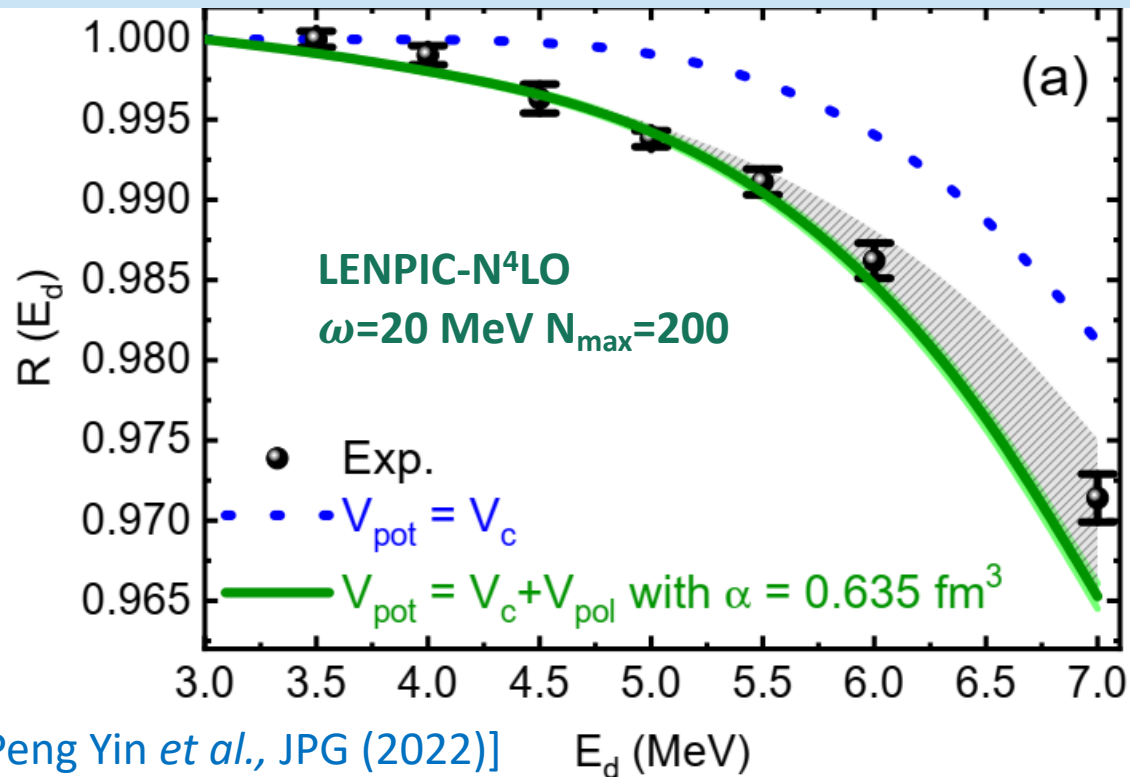
- ❖ Weijie Du, Peng Yin, Yang Li, Guangyao Chen, Wei Zuo, Xingbo Zhao, and James P. Vary, *Phys. Rev. C* **97**, 064620 (2018);
- ❖ Weijie Du, Peng Yin, Guangyao Chen, Xingbo Zhao, and James P. Vary, in *Proceedings of the International Conference "Nuclear Theory in the Supercomputing Era-2016" (NTSE-2016), Khabarovsk, Russia, September 19-23, 2016*;
- ❖ Peng Yin, Weijie Du, Wei Zuo, Xingbo Zhao and James P. Vary, *J. Phys. G* (2022)

Observables for $d+^{208}\text{Pb}$ scattering

$$R(E_d) = \frac{\sigma(E_d = 3 \text{ MeV}, \theta_1 = 60^\circ)}{\sigma(E_d = 3 \text{ MeV}, \theta_2 = 150^\circ)} \frac{\sigma(E_d, \theta_2 = 150^\circ)}{\sigma(E_d, \theta_1 = 60^\circ)}$$

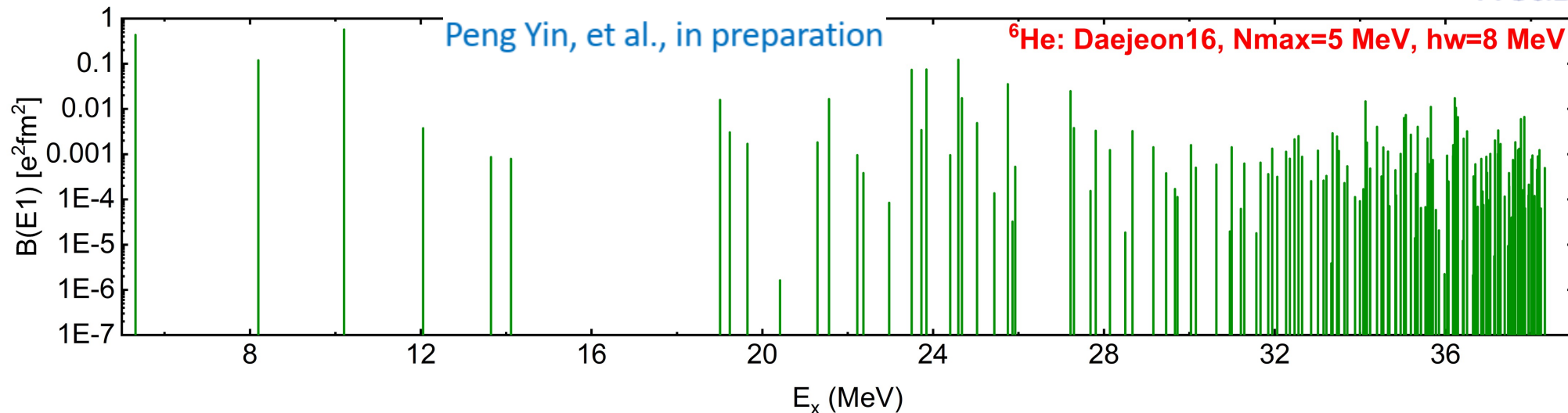
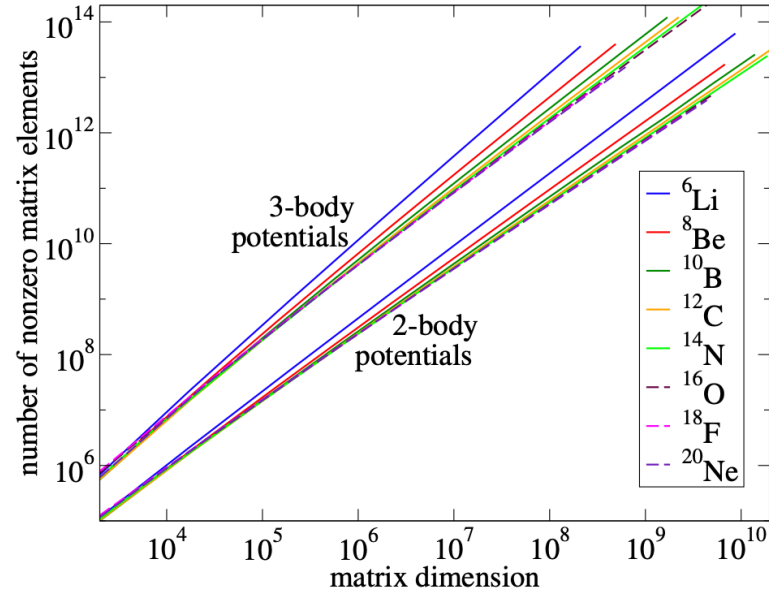
- ❖ Exp: N. L. Rodning, L. D. Knutson, W. G. Lynch and M. B. Tsang, Phys. Rev. Lett. 49, 909 (1982)
- ❖ No adjustable parameter
- ❖ No optical potential
- ❖ Energy loss correction

$$V_{\text{pol}} = -\frac{1}{2}\alpha Z^2 e^2 \frac{1}{r^4}$$



A > 2 projectile

- NCSM in HO basis with N_{\max} truncation; CoM motion; Pieter Maris (ISU), James P. Vary (ISU)
- Cori, Perlmutter, Sugon
- Calculate E1&M1 transition matrix elements
- One body density matrix elements (mixed parities, two independent runs)
- Postprocessor (manipulate wavefunctions), Patrick Fasano (UND) and Pieter Maris (ISU)
- Two-body operator (E1&M1) from LENPIC chiral EFT
- Application to tBF
- Photodisintegration of light nuclei



Conclusions/Perspectives

- ❖ Non-perturbative time-dependent basis function approach
- ❖ Application to $d+^{208}\text{Pb}$ scattering
- ❖ Extension of the tBF method to heavier projectiles, e.g., rare isotopes,... using wavefunctions from NCSM
- ❖ Extension to higher incident energies: adding strong interaction between scattering nuclei
- ❖ Two-body electromagnetic operators from chiral effective field theory
- ❖ Quantum consideration of center of mass motion of the projectile